

Effect of Decorrelation on Butterfly Search Velocity Estimator Performance

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ABSTRACT

The effect of signal decorrelation on the performance of the Butterfly Search velocity estimator is examined. An

analytical approximation for the expected value of the Butterfly Search $L(v)$ function is developed for three cases of interest. The approximations are verified against synthesized echo data. It is found that the peak value of the

where $h(t)$ is the two-way transfer function of the transducer. G is a scale factor, d_0 the depth at $n = 0$, c the speed

Doppler frequency shift of the signal.

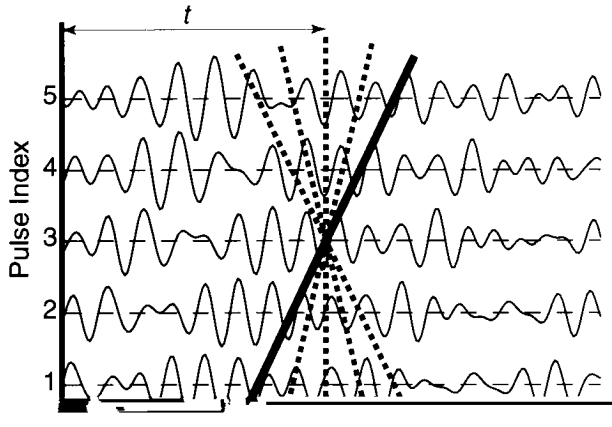
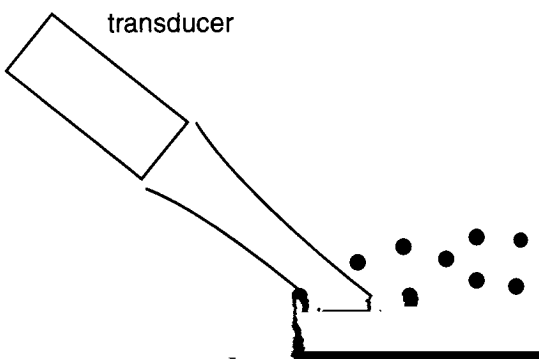
Equation 11 dependence on n is determined by the target velocity v . Any non zero velocity results in a time

Note that the left hand side is less than or equal to a constant. Since equality is achieved only when $g_1 = kg_2$, the left hand side will reach its peak only in the presence of a DC signal. Simplifying the above equation yields

Inserting the re-sampled signal $r_n(t, \nu)$ for g_1 finally gives the expression for $L(t, \nu)$

$$L(t, \nu) = \frac{\left| \sum_{n=0}^{N-1} r_n(t, \nu) \right|^2}{\sum_{n=0}^{N-1} |r_n(t, \nu)|^2} \quad (6)$$

This is the $L(\nu)$ function on RF of Alam and Parker, expanded as a function of time (depth). L takes on a maximum



Uncorrelated Noise The next degree of complexity involves a constant signal in the presence of noise. In this case, the random vector \mathbf{Z} is described by

where a is a real constant, and $\zeta_i = x_i + jy_i$, where x and y are independent Gaussian random variables, with zero mean and variance σ^2 , representing additive noise. The expression for the expected value of L may be written

$$E\{L\} = 1 + \sum_{i=1}^{n-1} \sum_{j=i+1}^n \left(E\{2a^2\} + E\{a\zeta_i + a\zeta_i^*\} + E\{a\zeta_j + a\zeta_j^*\} + E\{\zeta_i^*\zeta_j + \zeta_i\zeta_j^*\} \right) \quad (13)$$

The expression for the expected value is then

$$\frac{1}{\sqrt{(z_i^* z_j + z_j z_i^*) (z_i^* s_j + z_j s_i^*) (z_i^* s_j + z_j s_i^*) - (s_i^* s_j + s_j s_i^*)}}$$

The last three expected values can be taken to be zero. The leftmost expectation presents a problem in that the numerator and denominator terms are not independent. In order to attempt an analytical approximation, the

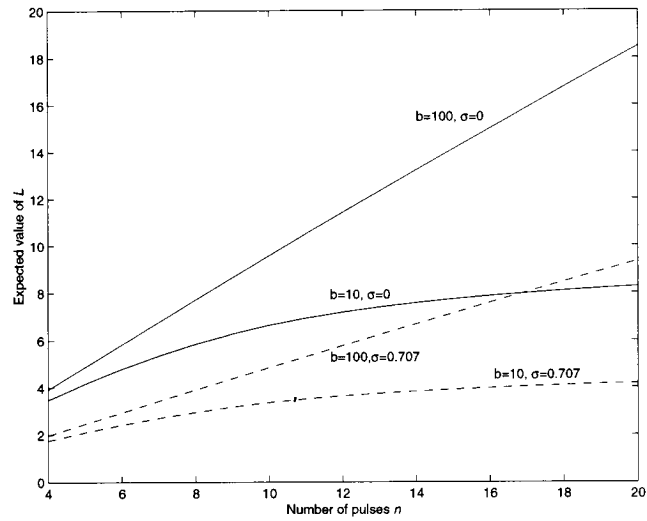


Figure 4. Expected value of L as a function of n . $a = 1$ for all traces.

Quantities to the performance of the Butterfly Search under these conditions a simulation study

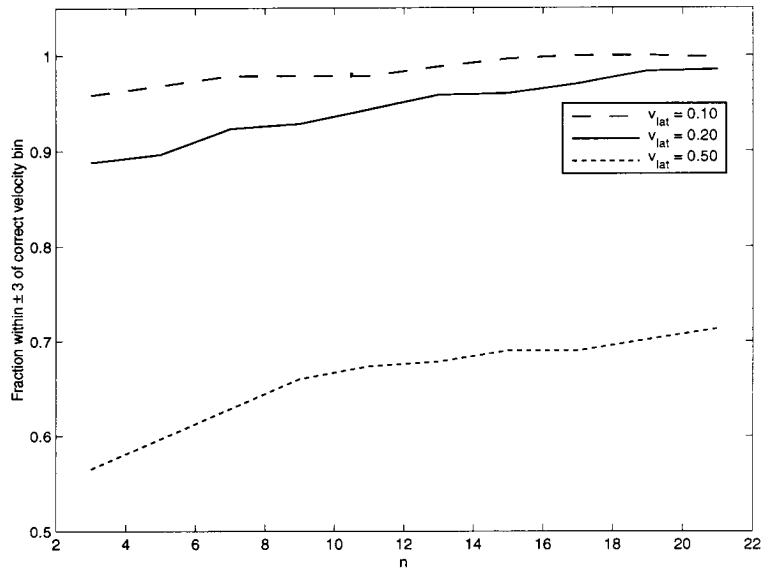
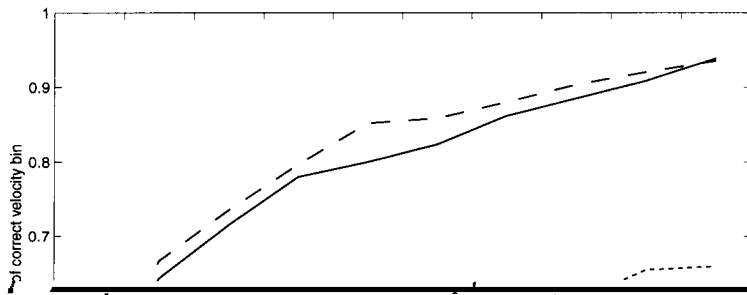


Figure 5. Fraction of velocity estimates within ± 3 velocity bins for lateral velocities of 0.1, 0.2 and 0.5 m/s, SNR = ∞



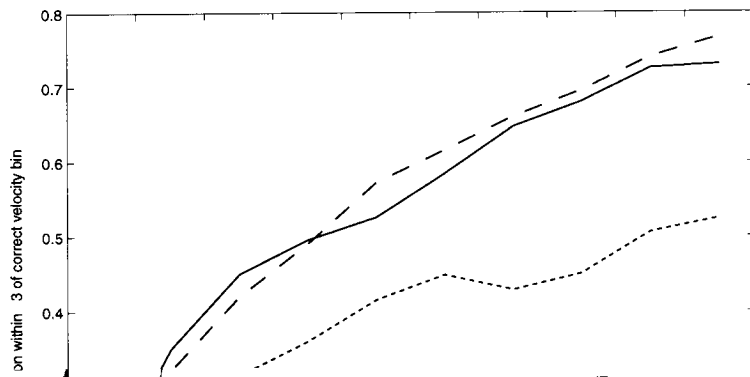
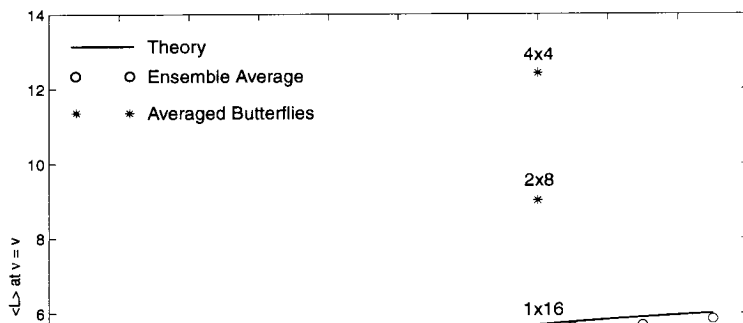


Figure 7. Fraction of velocity estimates within ± 3 velocity bins for lateral velocities of 0.1, 0.2 and 0.5 m/s, SNR = 0dB.



A-lines.

SNR = ∞

	$v_{\text{lateral}}(\text{m/s})$						
	0.00	0.01	0.02	0.05	0.10	0.20	0.50
1:16	1.00	1.00	1.00	1.00	1.00	0.96	0.69
2:8	1.00	1.00	1.00	1.00	1.00	0.97	0.72
4:4	1.00	1.00	1.00	1.00	1.00	1.00	0.86

SNR = 6dB

	$v_{\text{lateral}}(\text{m/s})$						
	0.00	0.01	0.02	0.05	0.10	0.20	0.50
1:16	0.88	0.89	0.90	0.90	0.89	0.88	0.63
2:8	0.81	0.84	0.84	0.82	0.83	0.87	0.63
4:4	0.72	0.73	0.72	0.73	0.76	0.82	0.71

SNR = 0dB

	$v_{\text{lateral}}(\text{m/s})$						
	0.00	0.01	0.02	0.05	0.10	0.20	0.50
1:16	0.69	0.71	0.70	0.69	0.68	0.67	0.42
2:8	0.58	0.61	0.63	0.60	0.59	0.64	0.44

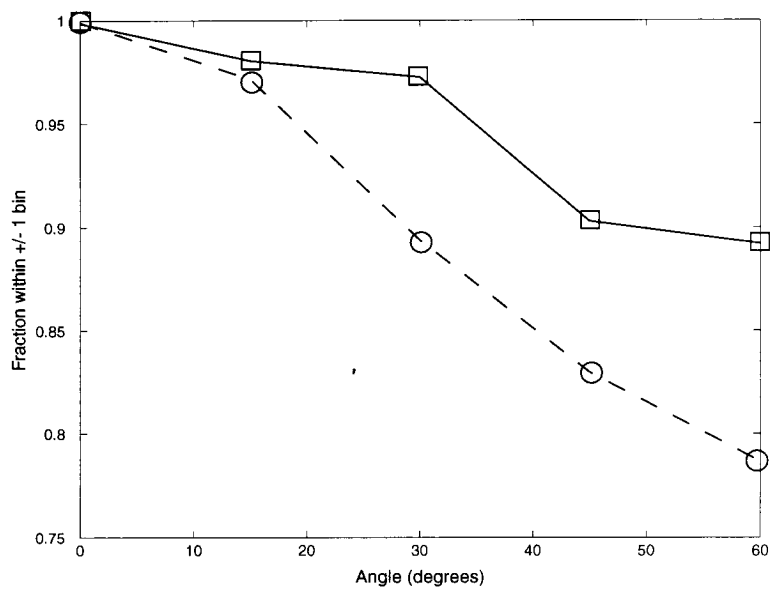


Figure 9. Performance of Butterfly estimator on water tank data versus angle. Circles denote data points for calculation using a one Butterfly of 16 A-lines. Squares indicate results for the average of four Butterflies of four

A-lines each..

5. CONCLUSION

The effect of echo-to-echo decorrelation on Butterfly Search estimation has been assessed. An analytical approximation to the expected value of the L function has been found for several cases of interest, and all are found to be in good agreement with results obtained by ensemble averaging. The approximations indicate that the maximum value of the L function is limited by the rate of signal decorrelation. Simulations show that this correlates well with

